15MAT41

# Fourth Semester B.E. Degree Examination, June/July 2017 Engineering Mathematics–IV

**CBCS** Scheme

Time: 3 hrs.

USN

Max. Marks: 80

Note: 1. Answer FIVE full questions, choosing one full question from each module. 2. Use of statistical tables are permitted.

### Module-1

- 1 a. Find by Taylor's series method the value of y at x = 0.1 from  $\frac{dy}{dx} = x^2y 1$ , y(0) = 1 (upto 4<sup>th</sup> degree term). (05 Marks)
  - b. The following table gives the solution of  $5xy' + y^2 2 = 0$ . Find the value of y at x = 4.5using Milne's predictor and corrector formulae. (05 Marks)

Х	4	4.1	4.2	4.3	4.4	
У	1	1.0049	1.0097	1.0143	1.0187	

- c. Using Euler's modified method. Obtain a solution of the equation  $\frac{dy}{dx} = x + |\sqrt{y}|$ , with initial conditions y = 1 at x = 0, for the range  $0 \le x \le 0.4$  in steps of 0.2. (06 Marks)
- 2 a. Using modified Euler's method find y(20.2) and y(20.4) given that  $\frac{dy}{dx} = \log_{10}\left(\frac{x}{y}\right)$  with y(20) = 5 taking h = 0.2. (05 Marks)

OR

- b. Given  $\frac{dy}{dx} = x^2(1+y)$  and y(1) = 1, y(1.1) = 1.233, y(1.2) = 1.548, y(1.3) = 1.979. Evaluate y(1.4) by Adams-Bashforth method. (05 Marks)
- c. Using Runge-Kutta method of fourth order, solve  $\frac{dy}{dx} = \frac{y^2 x^2}{y^2 + x^2}$  with y(0) = 1 at x = 0.2 by taking h = 0.2 (06 Marks)

## Module-2

3 a. Obtain the solution of the equation  $2\frac{d^2y}{dx^2} = ux + \frac{dy}{dx}$  by computing the value of the dependent variable corresponding to the value 1.4 of the independent variable by applying Milne's method using the following data: (05 Marks)

	X	1	1.1	1.2	1.3
	y	2	2.2156	2.4649	2.7514
	y'	2	2.3178	2.6725	3.0657
Express $f(x) = 3x^3 - $	$x^{2} + 5x -$	-2 in ter	ms of Lege	ndre polyr	omials.

(05 Marks)

c. Obtain the series solution of Bessel's differential equation  $x^2y'' + xy' + (x^2 + n^2)y = 0$ (06 Marks)

b.

# 15MAT41

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4	a.	By Runge-Kutta method solve $\frac{d^2y}{dx^2} = x\left(\frac{dy}{dx}\right)^2 - y^2$ for $x = 0.2$ . Correct to for	ur decimal
		places using the initial conditions $y = 1$ and $y' = 0$ at $x = 0$ , $h = 0.2$ .	(05 Marks)
	b.	Prove that $J_{+\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \sin x$	(05 Marks)
	c.	Prove the Rodrigues formula,	
		$\rho_{n}(x) = \frac{1}{2^{n} n!} \frac{d^{n} (x^{2} - 1)^{n}}{dx^{n}}$	(06 Marks)
		Module-3	
5	a.	State and prove Cauchy's-Riemann equation in polar form.	(05 Marks)
	b.	Discuss the transformation $W = e^z$ .	(05 Marks)
	c.	Evaluate $\int_{C} \left\{ \frac{\sin(\pi z^2) + \cos(\pi z^2)}{(z-1)^2(z-2)} \right\} dz$	
		using Cauchy's residue theorem where 'C' is the circle $ z  = 3$	(06 Marks)
		OR	
6	a.	Find the analytic function whose real part is, $\frac{\sin 2x}{\cosh 2y - \cos 2x}$ .	(05 Marks)
	b.	State and prove Cauchy's integral formula.	(05 Marks)
	c.	Find the bilinear transformation which maps $z = \infty$ , i, 0 into $\omega = -1$ , -i, 1. Also fin points of the transformation.	nd the fixed (06 Marks)
		Module-4	
7	a.	Find the mean and standard deviation of Poisson distribution.	(05 Marks)
	b.	In a test on 2000 electric bulbs, it was found that the life of a particular make wa	as normally
		distributed with an average life of 2040 hours and S.D of 60 hours. Estimate the	e number of
		(i) more than 2150 hours.	
		(ii) less than 1950 hours	
		(iii) more than 1920 hours and less than 2160 hours.	
	0	[A(1.833) = 0.4664, A(1.5) = 0.4332, A(2) = 0.4772] The joint probability distribution of two random variables x and y is as follows:	(05 Marks)
	C.	The joint probability distribution of two random variables x and y is as follows. x/y -4 2 7	
		$1 \frac{1}{18} \frac{1}{14} \frac{1}{18}$	
		5 1/4 1/8 1/8	
		Determine:	
		(i) Interginal distribution of x and y. (ii) Covariance of x and y	
		(iii) Correlation of x and y.	(06 Marks)

### **15MAT41**

a. The probability that a pen manufactured by a factory be defective is  $\frac{1}{10}$ . If 12 such pens are 8 manufactured what is the probability that, (i) Exactly 2 are defective (ii) at least 2 are

defective (iii) none of them are defective. (05 Marks) (05 Marks)

- b. Derive the expressions for mean and variance of binomial distribution.
- c. A random variable X take the values -3, -2, -1, 0, 1, 2, 3 such that P(x = 0) = P(x < 0) and P(x = -3) = P(x = -2) = P(x = -1) = P(x = 1) = P(x = 2) = P(x = 3). Find the probability distribution. (06 Marks)

#### **Module-5**

- In 324 throws of a six faced 'die' an odd number turned up 181 times. Is it reasonable to 9 a. think that the 'die' is an unbiased one? (05 Marks)
  - b. Two horses A and B were tested according to the time (in seconds) to run a particular race with the following results:

Horse A:	28	30	32	33	33	29	34
Horse B:	29	30	30	24	27	29	

Test whether you can discriminate between the two horses. ( $t_{0.05}=2.2$  and  $t_{0.02}=2.72$  for 11 d.f) (05 Marks)

c. Find the unique fixed probability vector for the regular stochastic matrix,  $A = \begin{vmatrix} y_6 & y_2 & y_3 \end{vmatrix}$ 

(06 Marks)

0 1 0

#### OR

- (ii) Type-I and Type-II error (iii) Confidence Define the terms: (i) Null hypothesis 10 a. (05 Marks) limits.
  - Prove that the Markov chain whose t.p.m  $P = \begin{vmatrix} 0 & \frac{2}{3} & \frac{1}{3} \\ \frac{1}{2} & 0 & \frac{1}{2} \end{vmatrix}$  is irreducible. Find the b. 1/2 1/2

corresponding stationary probability vector.

Three boys A, B, C are throwing ball to each other. A always throws the ball to B and B C. always throws the ball to C. C is just as likely to throw the ball to B as to A. If C was the first person to throw the ball find the probabilities that after three throws (i) A has the ball. (ii) B has the ball. (iii) C has the ball. (06 Marks)

\* \* \* \*

(05 Marks)



(12 Marks)

### Module-2

12kN

Fig.Q2(b)

- 3 a. Derive the differential equation of deflected curve for the beam. (04 Marks)
  - b. Determine the maximum deflection at the free end of a cantilever beam subjected point load W at free end of span 'L' with constant EI. Use Macaulay's method. (06 Marks)
     a. Using appropriate beam method, find the deflection at and of a cantilever beam of such that the deflection of a cantilever beam of such that the deflection of a cantilever beam of such that the deflection of a cantilever beam subjected point load (06 Marks)
  - c. Using conjugate beam method, find the deflection at end of a cantilever beam of span 'L' subjected udl of ω/mt run over entire span. EI constant. (06 Marks)

4 a. State first and second moment area theorems.

- (04 Marks)
- b. Find the ratio of deflection at C and D for the simply supported beam shown in Fig.Q4(b). Take E = 200 GPa,  $I = 6 \times 10^7$  mm<sup>4</sup>. Use Macaulay's method.



(05 Marks)

 c. Find the maximum deflection for the simply supported beam loaded as shown in Fig.Q4(c). Use moment-area method. (07 Marks)

#### Module-3

5 a. Derive the expression for the strain energy stored in a beam due to flexure. (04 Marks)
b. Find the horizontal and vertical deflection at the free end 'c' of a bent frame loaded as



(12 Marks)

OR

6 a. For the truss shown in Fig.Q6(a), determine the vertical deflection at C by strain energy method. Take E = 210 GPa and  $A = 5 \times 10^4$  mm<sup>2</sup>.



(09 Marks)

b. A cantilever beam is loaded as shown in Fig.Q6(b). Compute the deflection at point C by unit load approach. Take E = 200 GPa,  $I = 8 \times 10^7$  mm<sup>4</sup>.



(07 Marks)

- A three hinged parabolic arch of span 30 m, rise 5m is subjected to uniformly distributed load of 20 kN/m for left half of the span. Determine support reactions at the springing levels. Also determine normal thrust, radial shear and bending moment at a section 8 m from left support. (09 Marks)
  - b. A suspension cable of span 100 m and slip 10 m carries a udl of 8 kN/m of horizontal span over the entire span. Find the maximum and minimum tension in the cable and where they occur in the cable. Find the length of cable. (07 Marks)

#### OR

- 8 a. A flexible suspension cable of weight 12 kN/m hangs between two vertical walls 60 mt apart, left being at a point 10 m below the right point. A point load of 200 kN is attached to cable in such a manner that the point of attachment of load is 20 m horizontally from left end wall and 5 m below the left hand support. Find the maximum and minimum tension in the cable.
  - b. A parabolic arch of span 24 m with a central rise of 4 m is subjected to a point load of 30 kN at 6 m from left support and a udl of 15 kN/m over the right half of the span. Sketch BMD, also find normal thrust and radial shear at 10 m from right support. (08 Marks)

### Module-5

- 9 a. What are the uses of influence line diagram?
  - b. A simply supported beam of span 8m in traversed by a udl of 10 m long with intensity 20 kN/m. Draw the influence line diagram for:
    - i) Reaction at left support
    - ii) S.F at 3 mt from left support

iii) BM at 3 mt from left support.

Find the maximum values of above quantities.

#### OR

- 10 a. A beam has a span of 20 m. Draw influence line for BM and SF at a section 8m from the left support and determine the maximum BM and SF for this section due to two point loads 80 kN and 40 kN at a fixed distance of 2m apart rolling from left to right with 80 kN load leading.
  - b. Draw influence line for shear force and bending moment at a section 5 m from left support of a simply supported beam, 25 m long. Hence calculate the maximum SF and BM at this section due to uniformly distributed rolling load of 8m long with intensity 5 kN/m. (10 Marks)

3 of 3

(13 Marks)

(03 Marks)



b. A rectangular channel with bottom width 4m and bed slope 0.0008 has a discharge of  $1.5m^3/s$ . In a GVF in this channel the depth at a certain section is 0.3m. If n = 0.016, determine the type of profile. (08 Marks)

- 6 a. Explain the classification of surface profiles in an open channel with neat sketches.
  - b. A rectangular channel 8m wide discharges water with a depth of 0.4m and 6m/s velocity. Find the formation of hydraulic jump and if so, determine jump height and energy loss in meters.
     (06 Marks)

- a. Show that the maximum efficiency of jet striking at the center of a symmetrical single curved vane is  $\left(\frac{16}{27}\right)$  vane is semicircular. (08 Marks)
  - b. A Pelton wheel turbine has to be designed for the following : Data: Power = 6000kW, Net head = 300m, Speed = 550rpm, Jet ratio = 1/10, Overall efficiency = 85%, C<sub>v</sub> = 0.98, Speed ratio is 0.46. Determine diameter of runner and jet, discharge and number of jets required.

### OR

- a. Draw a neat sketch of a layout of hydroelectric power plant and explain the functions of each component. Also define different heads. (08 Marks)
  - b. A jet of water moving at 30m/s impinges on a series of curved vanes moving with a velocity of 15m/s. The jet makes an angle of 30° to the direction of motion of vane when entering and leaves at an angle of 120° to the direction of motion of vanes. Draw the velocity triangles at inlet and outlet and find :
    - i) The vane angle at inlet and outlet
    - ii) Workdone per N of water
    - iii) Hydraulic efficiency.

#### Module-5

a. Define :

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- i) Unit head ii) Unit discharge iii) Unit power (03 Marks)
   b. Derive the expression for minimum starting speed of a centrifugal pump. (06 Marks)
   c. A Kaplan turbine runner is to be designed to develop 7350kW power under a head of 5.5m
  - with  $\eta_0 = 85\%$ . Boss diameter =  $\frac{1}{3}$  diameter of runner, speed ratio = 2.1, Flow ratio = 0.7.

Determine :

i) Diameter of runner and boss, ii) Speed.

(07 Marks)

(06 Marks)

(08 Marks)

#### OR

10 a. Define draft tube. Explain its function. Draw the neat sketches of types of draft tubes.

- b. Define: i) Manometric head ii) Static head iii) Suction head iv) Delivery head.
- c. A centrifugal pump runs at 1000rpm and delvers water against a head of 15m. The impeller diameter and width at the outlet are 0.3m and 0.05m respectively. The vanes are curved back at 30°  $\eta_{man} = 92\%$ . Find discharge. (06 Marks)

2 of 2

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			CBCS Scheme	
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			Fourth Semester B.E. Degree Examination, June/July 2017	7
			Concrete Technology	
	Tin	ne: 3	3 hrs. Max. M	larks: 80
tetice.		3	Note: 1. Answer FIVE full questions, choosing one full question from each mod 2. Use of IS – 10262 – 2009 is permitted.	ule.
ated as malpra	1	a. b.	<u>Module-1</u> Write the chemical composition of cement. Write the flow chart for dry process. Explain the importance of size, shape and texture of aggregate.	(08 Marks) (08 Marks)
ng blank pages. 8 = 50, will be treat	2	a. b.	<b>OR</b> Explain the role of Admixtures in Concrete Technology. Name any four types of cement. State the properties and applications of any two cement.	(08 Marks) vo types of (08 Marks)
es on the remain s written eg, 42+	3	a. b.	Module-2 Define Workability. Explain the factors influencing workability of concrete. Write note on Segregation and Bleeding.	(08 Marks) (08 Marks)
igonal cross line ind /or equation	4	a. b.	OR Why curing is needed to concrete? Explain curing methods. Why compaction is required to concrete? Explain Compaction methods by vibration	(08 Marks) ion. (08 Marks)
lsorily draw dia il to evaluator a	5	a. b.	Module-3 Explain the factors influencing the strength of concrete. Write note on : i) Creep ii) Shrinkage of concrete.	(08 Marks) (08 Marks)
mpleting your answers, compu vealing of identification, appe-	6	a. b.	<b>OR</b> Explain Maturing concept of concrete. The strength of a sample of fully matured concrete is found to be 40MPa. Find to of identical concrete at the age of 7 days when cured at an average temperature time at 20 <sup>o</sup> C and night time at 10 <sup>o</sup> C. Take A = 32, B = 54.Use % strength of maturity = A + B log <sub>10</sub> $\left(\frac{\text{maturity}}{1000}\right)$ .	(08 Marks) the strength during day concrete at (08 Marks)
Important Note : 1. On con 2. Any re	7	De 102 a. b. c. d.	Module-4esign a concrete mix for $M_{20}$ grade of concrete with the following design stipulation $262 - 2009$ guide lines.Grade designation: M20.Type of cement : Ultra Tech PPC.Maximum size of Aggregate [MSA] : 20mmMinimum cement content : 320 kg/m <sup>3</sup> .Maximum W/C ratio : 0.55	as per IS

- a. Grade designation: M20.
  b. Type of cement : Ultra Tech PPC.
  c. Maximum size of Aggregate [MSA] : 20mm
  d. Minimum cement content : 320 kg/m<sup>3</sup>.
- e.
- Maximum W/C ratio : 0.55. Workability : 50 75mm (slump) f.

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### 15CV/CT44

- g. Exposure condition : Mild
- h. Degree of supervision : Good.
- i. Type of Aggregate : Crushed angular aggregate.
- j. Max. cement content :  $450 \text{ kg/m}^3$ .
- k. Chemical Admixture : Not recommended.
- 1. Specific gravity of cement : 3.05.
- m. Specific gravity of Coarse Aggregate : 2.68.
- n. Specific gravity of Fine Aggregate : 2.66.
- o. Water absorption of Coarse Aggregate : 0.85%.
- p. Water absorption of Fine Aggregate : 1.15%.
- q. Free (surface) moisture of Coarse Aggregate : NIL.
- r. Free moisture of Fine Aggregate : NIL.
- s. Sieve Analysis of Coarse Aggregate : Conforming to table 2 of IS : 383.
- t. Sieve Analysis of Fine Aggregate : Conforming to zone II of IS : 383.

### OR

8 What is meant by concrete mix design? Write the steps involved in the method of mix design (IS -10262 - 2009). (16 Marks)

#### Module-5

9	a.	Explain the materials used for self – compacting concrete.	(08 Marks)
	b.	State the advantages and disadvantages of RMC.	(08 Marks)

#### OR

10 a. Explain the fiber types used in Fiber Reinforced Concrete.b. State the advantages of Light Weight Concrete.

(08 Marks) (08 Marks)

(16 Marks)

2 of 2

	<b>CBCS</b> Scheme	
USN		15CV45
	Fourth Semester B.E. Degree Examination, June/July 2017	
	<b>Basic Geotechnical Engineering</b>	
Time	e: 3 hrs. Max. Ma	arks: 80
	Note: 1. Answer FIVE full questions, choosing one full question from each modu 2. Assume missing data, if any, suitably.	le.
	Module-1	
1	a. With the help of phase diagram of sol, define the terms:	
	1) Void ratio 11) Water content iii) Degree of saturation iv) Unit weight of sail	(00 Maalaa)
1	b. Following results were obtained from liquid limit test on a clay sample, whose pl	astic limit
	is 13% and natural water content is 18%. Determine the following:	
	1) Liquid limit ii) Flow index iii) Consistency index	
	Water content % 32 27.8 25.5 23.3	
,		(08 Marks)
	OR	
2	a. Sketch a typical grain-size curve for (i) Well graded soil, (ii) Uniformly gr	aded soil.
	Calculate uniformity coefficient and coefficient of curvature from the curve.	(04 Marks)
1	b. Explain the salient features of I.S. plasticity chart for classification of fine grained	soils. (06 Marks)
	c. A partially saturated sample from a borrow pit has a natural water content of 14%	6 and bulk
	unit weight of 19 kN/m <sup>3</sup> . The specific gravity of solids is 2.70. Determine the void	ratio, and
	degree of saturation. What will be the unit weight of the sample on saturation?	(06 Marks)
	Module-2	
3	a. Distinguish between: i) Primary and secondary valence bonds	
	ii) Dispersed and flocculent structures	
	iii) Structure of Kaolinite and Montmorillonite	
1	iv) Isomorphism substitution and base exchange capacity	(10 Marks)
i i	b. Differentiate between standard and modified proctor tests.	(06 Marks)
	OR	
4	a. Explain the factors affecting the degree of compaction.	(04 Marks)
	c. In a standard proctor test. Following results were obtained:	(04 Marks)
	Mass of compacted soil in grams 1700 1890 2003 1960	
	Water content %         7.7         11.5         14.6         19.7	
	<ul> <li>Draw the compaction curve showing OMC and maximum dry density.</li> <li>Determine the void ratio and degree of saturation</li> </ul>	
	Given, volume of mould = $950 \text{ cc}$ and $G = 2.65$ .	(08 Marks)
	1 of 2	

9

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- a. Define Darcy's law. Derive an expression to relate discharge velocity and seepage velocity. 5
  - b. Explain the following terms:
    - i) Total stress ii) Neutral stress
    - iii) Effective stress
- iv) Quick sand condition
- (06 Marks) c. An earthen dam is built on a impervious foundation with a horizontal filter under the downstream slope. The horizontal and vertical permeability of the soil material in the dam are respectively  $4 \times 10^{-5}$  m/sec and  $1 \times 10^{-5}$  m/sec. Full reservoir level is 20m above downstream filter. Flow net consists of 4 flow channels and 15 equipotential drops. Estimate the seepage loss per meter length of the dam. (04 Marks)

#### OR

- a. List the properties and use of flow nets. 6
  - In a falling head permeameter test, the initial head is 300 m it drops by 1 cm in 3 minutes. b. How much longer should the test to be continued, if the head is to drop to 180 m? (04 Marks)
  - Explain with neat sketch the method of locating the phreatic line in a homogenous earth dam with horizontal filter. (08 Marks)
    - **Module-4**
- 7 8 Explain mass-spring analogy of consolidation of soils.
  - In a consolidation test, the void ratio of soil sample decreases from 1.20 to 1.10 when the b. pressure increases from 160 to 320 kN/m<sup>2</sup>. Determine the coefficient of consolidation, if the coefficient of permeability is  $8 \times 10^{-7}$  mm/sec. (08 Marks)

#### OR

#### 8 Explain under consolidated, normally consolidated and over consolidated soil. a. (06 Marks)

- b. How preconsolidation pressure is determined by Casagrande's method? (06 Marks)
- A soil sample 2 cm thickness take 20 minutes to reach 20% consolidation. Find the time for C. a clay layer 6 cm thick to reach 40% consolidation. Assume double drainage in both cases. (04 Marks)

#### Module-5

Briefly explain Mohr-Coulomb's shear strength theory. a. (06 Marks) In a direct shear test on sand, sample failed at a shear strength of 70  $kN/m^2$  when normal b. stress was 100 kN/m<sup>2</sup>. Determine angle of internal friction. Draw Mohr circle at failure. Mark major and minor principal planes. What are the values of major and minor principal stresses? (10 Marks)

#### OR

- a. Mention the advantages and disadvantages of direct shear test. 10 (04 Marks)
  - Classify shear tests based on drainage conditions. b.
  - A soil has unconfined compression strength of 120 kN/m<sup>2</sup>. In triaxial compression test, C. specimen of same soil (under similar conditions) when subjected to cell pressure of 40 kN/m<sup>2</sup>, failed at an additional stress of 160 kN/m<sup>2</sup>. Determine:
    - i) Shear strength parameters

9

ii) Angle made by failure plane with axial stress direction in case of triaxial test. (09 Marks)

### 15CV45

(06 Marks)

#### (04 Marks)

### (08 Marks)

(03 Marks)



OR

- Azimuth iii) Altitude. (03 Marks) 6 Define the following : i) Vertical circle ii) a. (05 Marks) b. Explain Ecliptic and Solstices.
  - c. Find the shortest distance between two places A & B given that the longitudes of A and B are  $15^{\circ}$  0' N and  $12^{\circ}$  6' N and longitudes are  $50^{\circ}$  12' E and  $54^{\circ}$  0' E respectively. (08 Marks)

- Define the following terminologies : 7 a. i) Exposure station ii) Picture plane iii) Perspective centre. (03 Marks) b. Mention the general features of Photographic images. (07 Marks)
  - c. Find the number of photographers (size  $250 \times 250$  mm) required to cover over a area of 20km × 16km of the longitudinal overlap is 60% and the side overlap is 30% scale the (06 Marks) photograph is 1 cm = 150 m.

#### OR

(05 Marks) Derive an expression for relief displacement on a vertical photograph. 8 a. (05 Marks)

- b. Explain the procedure for aerial survey.
- c. A vertical photograph was taken at a altitude of 1200 meters above mean sea level. Determine the scale of the photograph for a terrain lying at elevations of 80 meters and 300 (06 Marks) meters if the focal length of the camera is 15cm.

#### Module-5

Mention the advantages of total station and also discuss the working principles of the same. 9 a.

(08 Marks)

Define Remote sensing. Explain the stages of idealized remote sensing system. (08 Marks) b.

#### OR

What is GIS? Enumerate on GIS applications in civil engineering. (08 Marks) 10 a. (08 Marks) Explain the basic principles of GPS and its application in surveying. b.





2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8=50, will be treated as malpractice. Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

### 15MATDIP41

**Module-3** 5 a. Find the Laplace transforms of : i)  $e^{-t}\cos^2 3t$  ii)  $\frac{\cos 2t - \cos 3t}{t}$ (06 Marks) b. Find: i)  $L\left[t^{-5/2} + t^{5/2}\right]$  ii)  $L[\sin 5t \cdot \cos 2t]$ . (05 Marks) c. Find the Laplace transform of the function :  $f(t) = E \sin\left(\frac{\pi t}{\omega}\right), 0 < t < \omega$ , given that  $f(t+\omega)=f(t).$ (05 Marks) OR a. Find : 6 i)  $L[t^2 \sin t]$  ii)  $L\left[\frac{\sin 2t}{t}\right]$ . (06 Marks) b. Evaluate :  $\int_{-\infty}^{\infty} \frac{\cos 6t - \cos 4t}{t} dt$  using Laplace transform. (05 Marks) c. Express  $f(t) = \begin{cases} \sin 2t, & 0 < t < \pi \\ 0, & t > \pi \end{cases}$ , in terms of unit step function and hence find L[f(t)]. (05 Marks) a. Solve the initial value problem  $\frac{\text{Module-4}}{\text{dx}^2} + \frac{5\text{dy}}{\text{dx}} + 6\text{y} = 5\text{e}^{2x}$ , y(0) = 2, y'(0) = 1 using Laplace 7 transforms. (06 Marks) b. Find the inverse Laplace transforms : i)  $\frac{3(s^2-1)^2}{2s^2}$  ii)  $\frac{s+1}{s^2+6s+9}$ . (05 Marks) c. Find the inverse Laplace transform :  $\log \left| \frac{s^2 + 4}{s(s+4)(s-4)} \right|$ . (05 Marks) OR a. Solve the initial value problem : 8  $\frac{d^2y}{dt^2} + \frac{4dy}{dt} + 3y = e^{-t}$  with y(0) = 1 = y'(0) using Laplace transforms. (06 Marks) b. Find the inverse Laplace transform : i)  $\frac{1}{s\sqrt{5}} + \frac{3}{s^2\sqrt{5}} - \frac{8}{\sqrt{5}}$  ii)  $\frac{3s+1}{(s-1)(s^2+1)}$ . (05 Marks) c. Find the inverse Laplace transform :  $\frac{2s-1}{s^2+4s+29}$ . (05 Marks)

### **15MATDIP41**

### Module-5

- 9 a. State and prove Baye's theorem.
  - b. A can hit a target 3 times in 5 shots, B 2 times in 5 shots and C 3 times in 4 shots. They fire a volley. What is the probability that i) two shots hit ii) atleast two shots hit? (05 Marks)
  - c. Find P(A), P(B) and P(A  $\cap \overline{B}$ ), if A and B are events with P(A  $\cup B$ ) =  $\frac{7}{8}$ ,  $P(A \cap B) = \frac{1}{4} \text{ and } P(\overline{A}) = \frac{5}{8}.$ (05 Marks)

#### OR

a. Prove that  $P(A \cup B) = P(A) + (B) - P(A \cap B)$ , for any two events A and B. 10 (06 Marks) Show that the events  $\overline{A}$  and  $\overline{B}$  are independent, if A and B are independent events. b.

(05 Marks) С. Three machines A, B and C produce respectively 60%, 30%, 10% of the total number of items of a factory. The percentage of defective output of these machines are respectively 2%, 3% and 4%. An item is selected at random and is found defective. Find the probability that the item was produced by machine C. (05 Marks)

(06 Marks)